ROBOT TEKNOLOJISI

Ege Üniversitesi Ege MYO Mekatronik Programı

BÖLÜM 3

Mobot (Mobil Robotlar)

Mobot: Mobil Robotlar

Mart 2013

İçerik

- Giriş
- Teker türleri
 - Fixed wheel
 - Centered orientable wheel
 - Off-centered orientable wheel
 - Swedish wheel
- Mobil Robot Hareketleri
 - Differential Drive
 - Tricycle
 - Synchronous Drive
 - Omni-directional
 - Ackerman Steering
- Mobil Robot kinematiği

Lokomosyon (Hareket Yeteneği)











Tekerlekli (Wheeled) Mobile Robotlar (WMR)



Yamabico



MagellanPro



Sojourner



ATRV-2



Hilare 2-Bis



Mobil Robotlar

- physical (hardware) and computational (software) components
- A collection of subsystems:
 - Locomotion: how the robot moves through its environment
 - Sensing: how the robot measures properties of itself and its environment
 - **Control:** how the robot generate physical actions
 - Reasoning: how the robot maps measurements into actions
 - Communication: how the robots communicate with each other or with an outside operator

Tekerlekli Mobil Robotlar

- Locomotion the process of causing an robot to move.
 - In order to produce motion, forces must be applied to the robot
 - Motor output, payload
- **Kinematics** study of the mathematics of motion without considering the forces that affect the motion.
 - Deals with the geometric relationships that govern the system
 - Deals with the relationship between control parameters and the behavior of a system.
- Dynamics study of motion in which these forces are modeled
 - Deals with the relationship between force and motions.

Notation



Posture: position(x, y) and orientation θ

{X_m,Y_m} – moving frame



robot posture in base frame

$$\mathsf{R}(\theta) = \begin{bmatrix} \cos\theta & \sin\theta & 0\\ -\sin\theta & \cos\theta & 0\\ 0 & 0 & 1 \end{bmatrix}$$

Rotation matrix expressing the orientation of the base frame with respect to the moving frame

Tekerlekler (Wheels)



Yönlendirilebilir Tekerlek (Steered Wheel)

- Yönlendirilebilir Tekerlek
 - Tekerleğin yönü denetlenebilir





İdeal Dönen Tekerlek



Non-slipping and pure rolling

- Kabuller
- 1. The robot is built from rigid mechanisms.
- No slip occurs in the orthogonal direction of rolling (non-slipping).
- 3. No translational slip occurs between the wheel and the floor (pure rolling).
- 4. The robot contains at most one steering link per wheel.
- 5. All steering axes are perpendicular to the floor.

Tekerlek Çeşitleri

Fixed wheel



Off-centered orientable wheel



Centered orientable wheel



Swedish wheel:omnidirectional property



Sabit Tekerlek

- Velocity of point P

 $\mathrm{V=}~(r\!\times\!\mathrm{w})a_x$

where, ax : A unit vector to X axis - Restriction to the robot mobility

Point \boldsymbol{P} cannot move to the direction perpendicular to plane of the wheel.



Merkezinden Denetlenebilir Teker

- Velocity of point P

$$V = (\mathbf{r} \times \mathbf{w}) \mathbf{a}_{\mathbf{x}}$$
whereaxis
$$a\mathbf{x} : A \text{ unit vector of } \mathbf{x}$$
axis
$$a\mathbf{y} : A \text{ unit vector of } \mathbf{y}$$
axis

Restriction to the robot mobility



Merkez dışından denetlenebilir Teker (caster wheels)

- Velocity of point P

$$v = (\mathbf{r} \times \mathbf{w})\mathbf{a}_{\mathbf{x}} + (\mathbf{d} \times \mathbf{t})\mathbf{a}_{\mathbf{y}}$$

$$where, \quad \mathbf{axis} \quad \mathbf{ax} : \text{A unit vector of } \mathbf{x}$$

$$a\mathbf{y} : \text{A unit vector of } \mathbf{y}$$
- Restriction to the robot mobility



İsveç (Swedish) Tekerlek

- Velocity of point P

- Omnidirectional property



Örnek WMR



- Smooth motion
- Risk of slipping
- Some times use roller-ball to make balance
- Exact straight motion
- Robust to slipping
- Inexact modeling of turning
- Free motion
- Complex structure
- Weakness of the frame

Mobil Robot Yönlendirme

 Instantaneous center of rotation (ICR) or Instantaneous center of curvature (ICC)



Mobilite Derecesi

• Degree of mobility

The degree of freedom of the robot motion



Cannot move anywhere (No ICR)

• Degree of mobility :



Fixed arc motion (Only one ICR)

• Degree of mobility : 1



()

Variable arc motion (line of ICRs)

Degree of mobility :
 2



Fully free motion

(ICR can be located at any

• Degree of mobilition) 3

Yönlendirme derecesi

• Degree of steerability

The number of centered orientable wheels that can be steered independently in order

to steer



No centered orientable wheels

• Degree of steerability : 0

One centered orientable wheel



Two mutually dependent centered orientable wheels



Two mutually independent centered orientable wheels

Degree of steerability :
 1

• Degree of steerability : 2

Manevra derecesi

• Toplam bağımsız hareket edebilme derecesi:



Manevra derecesi

 $\delta_M = \delta_m + \delta_s$



Non-holonomic constraint

A non-holonomic constraint is a constraint on the feasible **velocities** of a body

So what does that mean?

Your robot can move in some directions (forward and backward), but not others (sideward).



Mobil Robot Yönlendirme

- Differential Drive
 - two driving wheels (plus roller-ball for balance)
 - simplest drive mechanism
 - sensitive to the relative velocity of the two wheels (small error result in different trajectories, not just speed)
- Steered wheels (tricycle, bicycles, wagon)
 - Steering wheel + rear wheels
 - cannot turn ±90°
 - limited radius of curvature
- Synchronous Drive
- Omni-directional
- Car Drive (Ackerman Steering)



- Posture of the Control input robot $P = \begin{pmatrix} x \\ y \\ \theta \end{pmatrix} \begin{pmatrix} (x,y) \\ \theta \end{bmatrix}$ Position of the θ robot : Orientation of the robot
 - *v* : Linear velocity of the **robot**
 - *w*: Angular velocity of the **robot**

(notice: not for each wheel)

 $V_R(t)$ – linear velocity of right wheel $V_L(t)$ – linear velocity of left wheel r – nominal radius of each wheel R – instantaneous curvature radius of the robot trajectory (distance from ICC to the midpoint between the two wheels).



Posture Kinematics Model: Kinematics model in world frame

- Relation between the control input and speed
- $\omega = \frac{V_R V_L}{L} \qquad v = \frac{V_R + V_L}{2}$ Kinematic equation

of $_{\rm W}V_L = r \omega_L$ $V_R = r \omega_R$

$$\begin{pmatrix} \vec{x} \\ \vec{y} \\ \vec{\theta} \end{pmatrix} = \begin{pmatrix} \cos\theta & 0 \\ \sin\theta & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} v \\ \boldsymbol{\omega} \end{pmatrix}$$

• Nonholonomic Constraint $\begin{bmatrix} \sin \theta & -\cos \theta \end{bmatrix} \begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \dot{x} \sin \theta$

$$\int_{x} \frac{Y_{1}}{y_{m}} \frac{y_{m}}{y_{m}} \frac{y_{r}}{y_{m}} \frac{y_{r$$

Kinematics model in robot frame ---configuration kinematics model

$$\begin{bmatrix} v_{x}(t) \\ v_{y}(t) \\ \dot{\theta}(t) \end{bmatrix} = \begin{bmatrix} r/2 & r/2 \\ 0 & 0 \\ -r/L & r/L \end{bmatrix} \begin{bmatrix} w_{1}(t) \\ w_{r}(t) \\ \end{bmatrix}$$

- w_r(t) angular velocity of right wheel
- w_I(t) angular velocity of left wheel

Basic Motion Control

Instantaneous center of rotation



$$V_R - V_L) / L = V_R / (R + \frac{L}{2})$$
$$R = \frac{L}{2} \frac{V_R + V_L}{V_R - V_L}$$
$$R : \text{Radius of rotation}$$

• Straight motion

 $R = Infinity \rightarrow V_R =$

• Rotational motion

$$R = 0 \rightarrow V_{R}$$
$$= -V_{L}$$

Basic Motion Control

• Velocity Profile

R

φ



- D rotation
- φ : Length of path
 - : Angle of rotation

- Three wheels and odometers on the two rear wheels
- Steering and power are provided through the front wheel
- control variables:
 - steering direction $\alpha(t)$
 - angular velocity of steering wheel $w_s(t)$



The ICC must lie on the line that passes through, and is perpendicular to, the fixed rear wheels

 If the steering wheel is set to an angle $\alpha(t)$ from the straight-line direction, the tricycle will rotate with angular velocity $\omega(t)$ about ICC lying a distance R along the line perpendicular to and passing through the rear wheels.





Kinematics model in the robot frame ---configuration kinematics model

$$v_{x}(t) = v_{s}(t) \cos \alpha(t)$$

$$v_{y}(t) = 0$$

$$\dot{\theta}(t) = \frac{v_{s}(t)}{d} \sin \alpha(t)$$

with no splippage

Kinematics model in the world frame ---Posture kinematics model



- In a synchronous drive robot (synchronous drive) each wheel is capable of being driven and steered.
- Typical configurations
 - Three steered wheels arranged as vertices of an equilateral
 - triangle often surmounted by a cylindrical platform
 - All the wheels turn and drive in unison
- This leads to a holonomic behavior



- All the wheels turn in unison
- All of the three wheels point in the same direction and turn at the same rate
 - This is typically achieved through the use of a complex collection of belts that physically link the wheels together
 - Two independent motors, one rolls all wheels forward, one rotate them for turning
- The vehicle controls the direction in which the wheels point and the rate at which they roll
- Because all the wheels remain parallel the synchro drive always rotate about the center of the robot
- The synchro drive robot has the ability to control the orientation θ of their pose directly.

- Control variables (independent)
 - $-v(t), \omega(t)$



- The ICC is always at infinity
- Changing the orientation of the wheels manipulates the direction of ICC

- Particular cases:
 - v(t)=0, w(t)=w during a time interval Δt , The robot rotates in place by an amount $w \Delta t$.
 - v(t)=v, w(t)=0 during a time interval Δt , the robot moves in the direction its pointing a distance $v \Delta t$.



Omidirectional





Swedish Wheel

Car Drive (Ackerman Steering)



- Used in motor vehicles, the inside front wheel is rotated slightly sharper than the outside wheel (reduces tire slippage).
- Ackerman steering provides a fairly accurate dead-reckoning solution while supporting traction and ground clearance.
- Generally the method of choice for outdoor autonomous vehicles.

Ackerman Yönlendirme



where

- d = lateral wheel separation
- l = longitudinal wheel separation
- θi = relative steering angle of inside wheel
- θo = relative steering angle of outside wheel
- R=distance between ICC to centerline of the vehicle

Ackerman Steering

• The Ackerman Steering equation:



Ackerman Yönlendirme

Equivalent:



Araba Benzeri Mobil Robot Kinematik modeli

- Control Input
- Driving type: Forward wheel drive



Araba Benzeri Mobil Robot Kinematik modeli



Dinamik Model



Özet

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- Tekerlek Çeşitleri
 - Fixed wheel
 - Centered orientable wheel
 - Off-centered orientable wheel (Caster Wheel)
 - Swedish wheel
- Mobil Robot Yönlendirme
 - Degrees of mobility
 - 5 types of driving (steering) methods
- WMR Kinematik
- Temel Denetim

